Mathematical Foundations of Machine Learning – Spring 2020

Summer Project list

General comments

- A. Use publically available datasets such as the UCI machine learning repository (<u>http://archive.ics.uci.edu/ml/index.php</u>)
- B. In all experiments use 5 fold cross validation.
- C. For regression problems provide average error and std of error statistics.
- D. For classification problems provide accuracy (TP+TN)/(P+N), precision TP/(TP+FP) and recall TP/(TP+FN) statistics.
- E. Perform hyper-parameter search and try to explain the logic of the best configuration.
- F. "Debug" your results: look at confusion matrices, investigate your false positive and negatives. Try to understand where your models fail and try to fix them.
- G. For ML problems, compare your results to the results using standard models from Scikit-Learn, R, etc.
- H. Try to come up with other ideas beyond the basic project description.
- 1. [Feature importance via wavelet decomposition of RF] Reproduce the feature importance results of [1]
 - a. Provide summary of the wavelet-based method with emphasis on the use of the validation set to determine a threshold for wavelet norms.
 - b. Test on regression & classification problems (multi-class problems).
 - c. Observe differences (if any) on small/large datasets.
 - d. Compare extensively with standard methods as in [1]
- 2. [Compression & denoising with wavelet decomposition of RF] Reproduce and add to the results of [1]
 - a. Compression Investigate the RF compression capabilities of wavelets through tradeoff between the number of trees and tree components versus the prediction error.
 - b. Denoising add various levels of Gaussian noise to regression datasets and add various levels of mis-labeling to classification datasets. Investigate the performance of wavelet denoising.
- 3. [Function space analysis of DL] Reproduce the research of the paper [3]
 - a. Train 'small' TensorFlow networks for MNIST, CIFAR10 datasets.
 - b. Perform Besov smoothness analysis of the representation layers at various stages of the training
 - c. Try also to experiment with different network configurations and investigate the relationship between the classification error on the testing set and the smoothness analysis of the representation layers.
- 4. [Function space analysis of ResNets] Add to the research of [3]
 - a. Train a 'small' version of a ResNet [4] on the CIFAR10 dataset.
 - b. Investigate the performance and perform Besov smoothness analysis of the network with and without the residual connections.

- 5. [Function space analysis of Transfer learning] Add to the research of [3]
 - a. Train a network on the MNIST dataset.
 - b. Perform Besov smoothness analysis.
 - c. Apply transfer learning on a 'small' set of (grayscale) CIFAR10 using as basis a network from (a). This implies 'freezing' some of the first layers and re-training the last layers or creating and training new last layers.
 - d. Perform Besov smoothness analysis of the transfer-learning architecture using the full CIFAR10 set.
- 6. [Deep neural decision forest] Follow [7] to create an architecture that combines CNN architecture with differentiable decision tree/forest
 - a. Use MNIST and CIFAR10 datasets.
 - b. Compare to the 'standard' architecture with the softmax layer.
- 7. [Scattering Networks for small datasets] Use the methods of [6] to compare the results of trained convolutional neural networks over Scattering Networks in the cases of small/simple datasets.
 - a. Use the MNIST dataset as an example for a 'simple' dataset.
 - b. Use various sizes of the CIFAR10 dataset.
- 8. [AI for numerical PDEs] Follow [8] to apply a DL solution to a PDE
 - a. Use example 3.1.1 of [8] as a base for your experiments.
 - b. Try examples where you know what the analytic solution is
 - c. Try to compare with other 'off-the-shelf' solvers.
- 9. [AI for numerical PDEs] Apply a DL approach to inverse problems of the wave equation
 - a. Create via simulations a dataset of waves with time [0,1000] and different source locations. Use as domain a square with a grid of 128x128.
 - b. Train a regression DL network on dataset of images at time 1000 to predict source location.
 - c. Train a regression DL network on dataset of images at various times [500,1000] to predict source location.

References

[1] O. Elisha and S. Dekel, Wavelet decompositions of Random Forests - smoothness analysis, sparse approximation and applications, JMLR 17 (2016).

[2] O. Morgan, O. Elisha and S. Dekel, Wavelet decomposition of Gradient Boosting, preprint.

[3] O. Elisha and S. Dekel, Function space analysis of deep learning representation layers, preprint.

[4] H. Kaiming, Z. Xiangyu, R. Shaoqing and SD Jian, Residual Learning for Image Recognition, proceedings of CVPR 2016.

[5] S. Mallat, Group Invariant Scattering, Comm. Pure and Applied Math 65 (2012), 1331-1398.

[6] J. Bruna and S. Mallat, Invariant Scattering Convolution Networks, IEEE Transactions on Pattern Analysis and Machine Intelligence 35 (2013), 1872 – 1886.

[7] P. Kontschieder, M. Fiterau, A. Criminisi and S. Rota Bul'o, Deep Neural Decision Forests, ICCV 2015.

[8] M. Raissia, P. Perdikarisb and G.E.Karniadakisa, Physics-informed neural networks: A deep learning framework for solving forward and inverse problems involving nonlinear partial differential equations, Journal of Computational Physics 378(2019), 686–707.